Complex Functions 2010: Hand-in exercise 7

March 14, 2010

1. Prove the theorem below, only using theory from pages $\leq 103 \ (4^{th} \text{ ed.})$. (Hint: study the proof of Goursat's Theorem, page 105)

Theorem: Let T be an isosceles rectangled triangle and let f be a complex function wich is holomorphic on T. Then

$$\oint_{\partial T} f = 0.$$

2. Define $f(z) := e^{iz^2}$ and consider the triangle with vertices 0, R, R + iR. Use the theorem above to prove that

$$\int_{-\infty}^{\infty} \sin{(t^2)} dt = \sqrt{\frac{\pi}{2}}.$$